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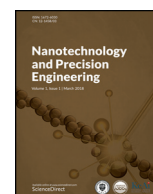
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Enhancement of surface wettability via micro- and nanostructures by single point diamond turning

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ABSTRACT

Studies on surface wettability have received tremendous interest due to their potential applications in research and industrial processes. One of the strategies to tune surface wettability is modifying surface topography at micro- and nanoscales. In this research, periodic micro- and nanostructures were patterned on several polymer surfaces by ultra-precision single point diamond turning to investigate the relationships between surface topographies at the micro- and nanoscales and their surface wettability. This research revealed that single-point diamond turning could be used to enhance the wettability of a variety of polymers, including polyvinyl chloride (PVC), polyethylene 1000 (PE1000), polypropylene copolymer (PP) and polytetrafluoroethylene (PTFE), which cannot be processed by conventional semiconductor-based manufacturing processes. Materials exhibiting common wettability properties ($\theta \approx 90^\circ$) changed to exhibit "superhydrophobic" behavior ($\theta \sim 150^\circ$). Compared with the size of the structures, the aspect ratio of the void space between micro- and nanostructures has a strong impact on surface wettability.

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1. Background

Surface behavior plays a key role in many physical or chemical properties such as wettability,¹ optical properties,² thermal emissivity,³ corrosion,⁴ and other biological and chemical processes.^{5–8} Wettability is the tendency of one fluid to spread on or adhere to a solid surface. Wettability can be measured by the contact angle, which is conventionally measured through the liquid, where a liquid–vapor interface meets a solid surface. Different theories have been proposed to explain wetting phenomena.⁹ Young defined the wettability for ideal surfaces as in Eq. (1).

$$\cos(\Theta_{\text{ideal}}) = \frac{\gamma_{\text{sv}} + \gamma_{\text{sl}}}{\gamma_{\text{lv}}} \quad (1)$$

where θ_{ideal} is the ideal contact angle, γ_{lv} is the surface tension of the liquid/vapor interface, γ_{sl} is the surface tension of the solid/liquid interface, and γ_{sv} represents the surface tension of the solid/vapor interface. Depending on the value of the contact angle, surfaces can be classified into four groups: superhydrophobic ($\theta > 150^\circ$), hydrophobic

($90^\circ < \theta < 150^\circ$), hydrophilic ($10^\circ < \theta < 90^\circ$), and superhydrophilic ($\theta < 10^\circ$).¹⁰

The wettability can also be researched by the advancing contact angle (θ_a), receding contact angle (θ_r), and hysteresis angle (θ_H). The advancing contact angle is a measure of the liquid–solid cohesion, whereas the receding contact angle is a measure of liquid–solid adhesion. Contact angle hysteresis can arise from molecular interactions between the liquid and solid or from surface anomalies, such as roughness or heterogeneities.¹¹ It is defined as the difference between the value of the angle of advance and the value of the receding contact angle (Eq. (2)).

$$\theta_H = \theta_a - \theta_r \quad (2)$$

Surface energy and topography are the main factors affecting wettability. Wettability has been widely researched as a function of surface texture, material's chemistry, and processing conditions.¹²

Surface topography can be altered modifying roughness.^{13,14} The presence of features on surfaces can lead to large values of hysteresis where substantial forces may be required to initiate drop movement.¹⁵ For very rough surfaces, drops can be suspended atop patterns, leaving air between them.¹⁶ This suspension enables to have substrates with superhydrophobic behavior where drops can roll easily on them behaving as self-cleaning surfaces.

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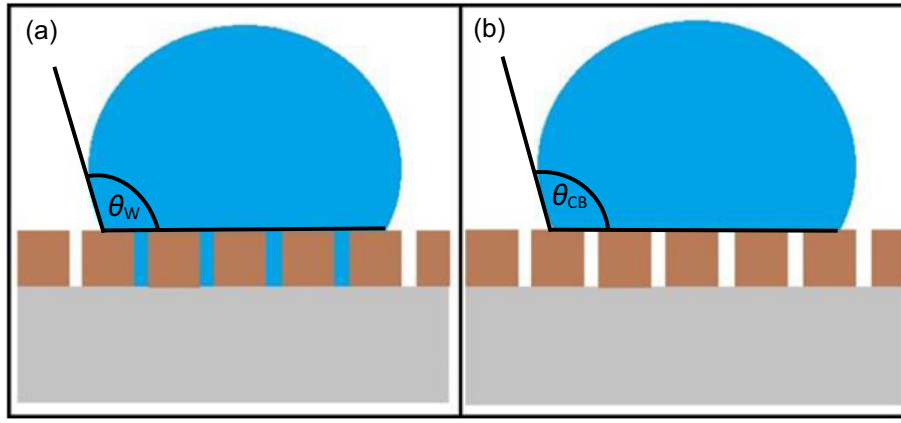


Fig. 1. Sketches of a liquid droplet in (a) the Wenzel state with an apparent contact angle θ_W and (b) the Cassie–Baxter state with an apparent contact angle θ_{CB} .

Wenzel and Cassie–Baxter created models for explaining wettability in real surfaces that exhibit some degree of roughness or are chemically heterogeneous. The Wenzel model supposes that a liquid can penetrate in the pores of the surface, and contact is homogeneous. Wenzel's equation is shown in Eq. (3):

$$\cos(\theta_W) = r \cdot \cos\theta_{ideal} \quad (3)$$

where θ_{ideal} is the contact angle in an ideal surface that cannot be practically obtained. θ_W is the contact angle in a real surface, and r is the Wenzel roughness factor. The factor r tries to explain that the roughness enhances the wettability properties of the smooth surfaces.

The Cassie–Baxter model describes heterogeneous wetting contact between the droplet and surface due to air entrapment. According to this theory, there is an area fraction where the liquid and solid are in contact and another area fraction where the liquid and gas stay in contact. The Cassie–Baxter model is defined in Eq. (4).

$$\cos(\theta_{CB}) = f_1 \cdot \cos\theta_1 + f_2 \cdot \cos\theta_2 \quad (4)$$

where θ_{CB} is the contact angle in a real surface, θ_1 and θ_2 are the contact angles of the two surfaces that are in contact (liquid–vapor and liquid–solid), and f_1 and f_2 are the apparent area fractions of surface components. Sketches of the Wenzel and Cassie–Baxter model are shown in Fig. 1.

The contact angle is generally expected to obey the Wenzel model on substrates with moderate roughness, and it follows Cassie–Baxter

behavior on highly rough surfaces. On hydrophobic surfaces ($\theta \approx 100^\circ$) of moderate roughness ($r_s \approx 2$), both Wenzel and Cassie–Baxter states can co-exist. Some researchers believe the wettability models are limited because they use contour area rather than the contact line.¹⁷

Superhydrophobic examples are found in lotus leaves¹⁸ and certain insects and birds¹⁹ where superhydrophobicity is achieved by surface textures consisting of micro- and nano-scale hierarchical structures. On the basis of these principles, two main strategies are developed for the preparation of superhydrophobic surfaces. One strategy consists of the deposition of hydrophobic materials that can be applied as coating layers such as poly(dimethylsiloxane) (PDMS)²⁰ or fluorinated silane compounds.²¹ This strategy is associated with certain disadvantages such as cost, long procedure, and problems with substrate biocompatibility. The other strategy consists of machining of patterns on the surfaces by photolithography and electron beam lithography.²² Photolithography has the disadvantage of limited choices in photoresist and substrate. Electron beam lithography presents the disadvantage of being a slow and expensive manufacturing technique that cannot be applied at a large scale.

Single point diamond turning (SPDT) is a versatile and highly controllable technique for manufacturing micro- and nanostructured surfaces with high accuracy. Compared with lithography technologies, SPDT can be used to machine a wide range of materials including polymers, metals, and ceramics, with high throughput at very large scales. This technique is based on turning with diamond as the cutting tool to mechanically remove materials with a precision in several nanometers

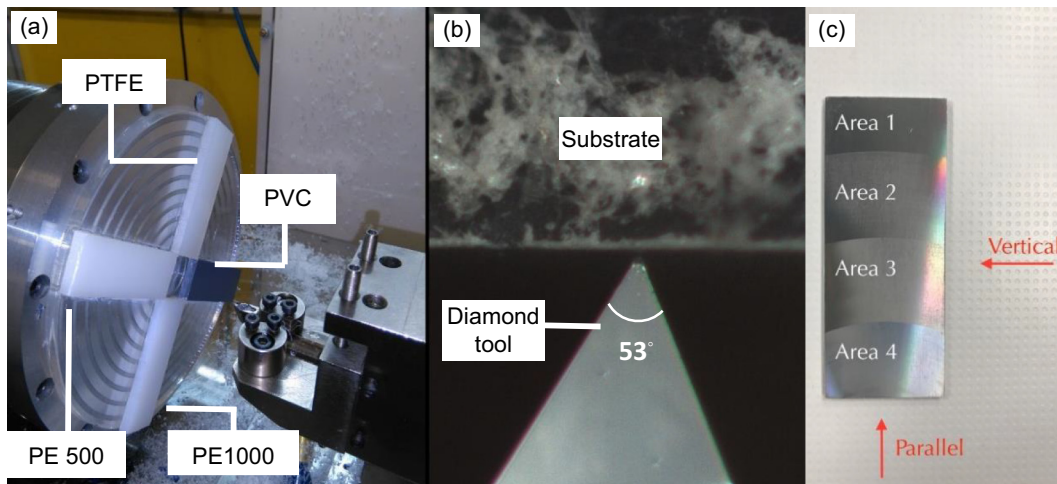


Fig. 2. Overall manufacturing process: (a) experimental setup of diamond turning process; (b) microscope image of the diamond cutting process; (c) an aluminum sample with four different structures in 4 μm (Area 1), 2 μm (Area 2), 1 μm (Area 3), and 500 nm (Area 4).

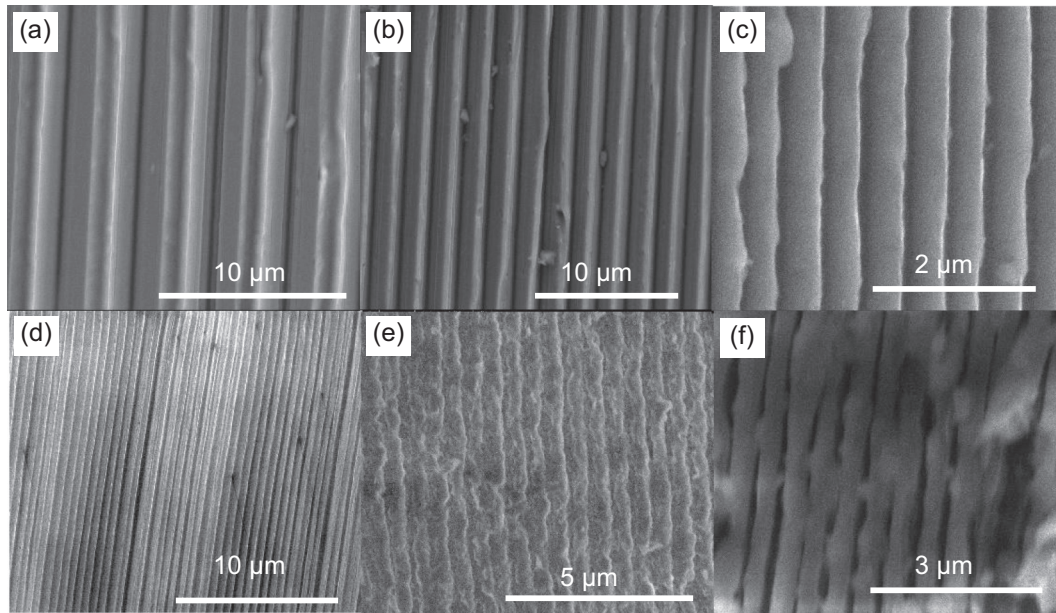


Fig. 3. SEM images of micro and nanostructures on different materials: (a) 4 μm gratings on aluminum; (b) 2 μm gratings on aluminum; (c) 0.5 μm gratings on aluminum; (d) 0.5 μm gratings on PE1000; (e) 0.5 μm gratings on PTFE; and (f) 0.5 μm gratings on PVC.

on a wide variety of materials. SPDT is affected by process and material factors. The material factors include material swelling and recovery, grain boundaries, material spring back, and minimum undeformed chip thickness.²³

Through manufacturing of micro- and nanostructures on a variety of materials by SPDT, this research aimed to investigate how surface topographies affect wettability in hydrophobic and hydrophilic regimes. For this reason, micro- and nanostructures on the surfaces of several materials, including aluminum, polyvinyl chloride (PVC), polyethylene, polypropylene copolymer, PFTE and polypropylene copolymer (PP), with feature dimensions from 500 nm to several micrometers, were employed. The surface of the different patterned areas and the wettability of these materials were characterized and analyzed. Finally, the

values of contact angles obtained for the different patterned and flat surfaces were compared, and the patterns' height was found to affect the wettability for these materials.

2. Experimental procedures

Through a customized five axis ultra-precision machine, micro- and nanogratings (500 nm, 1 μm , 2 μm , and 4 μm) were machined on materials including aluminum, PVC, polyethylene 1000 (PE 1000), polyethylene 500 (PE 500), polypropylene copolymer (PP), and PFTE. Under a spindle speed of 1000 rpm, feed rates of 4 mm/min, 2 mm/min, 1 mm/min, and 0.5 mm/min were employed to achieve 4 μm , 2 μm , 1 μm , and 0.5 μm per revolution. A sharp point diamond tool with

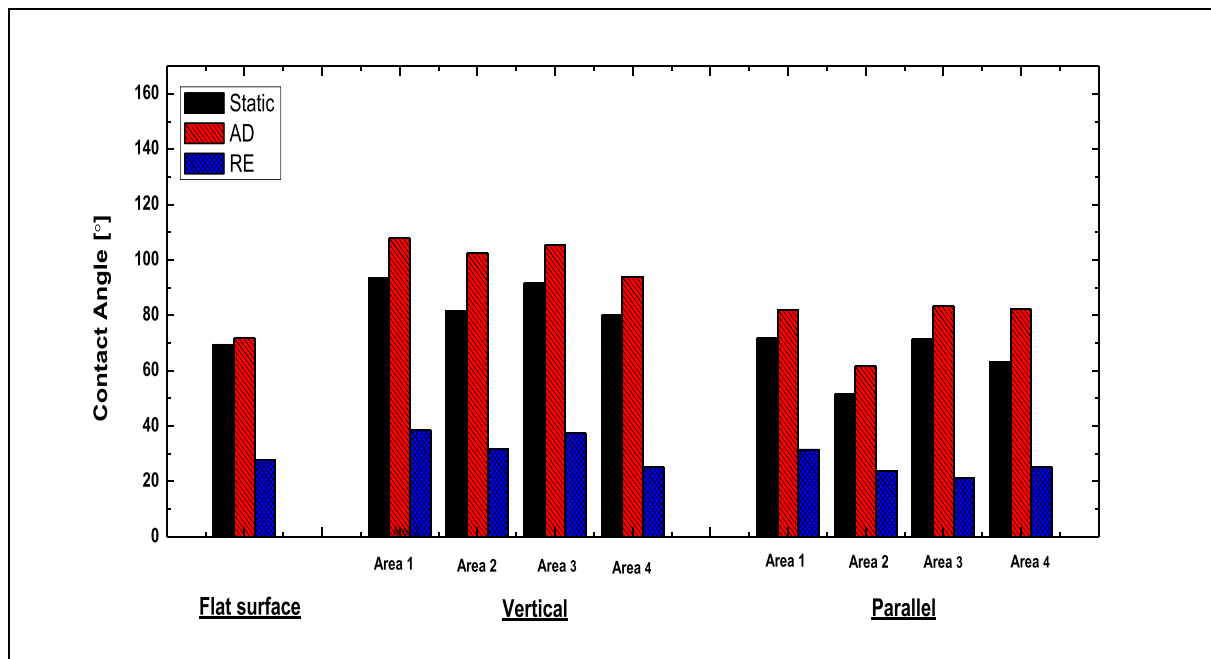


Fig. 4. Contact angle measurements for aluminum.

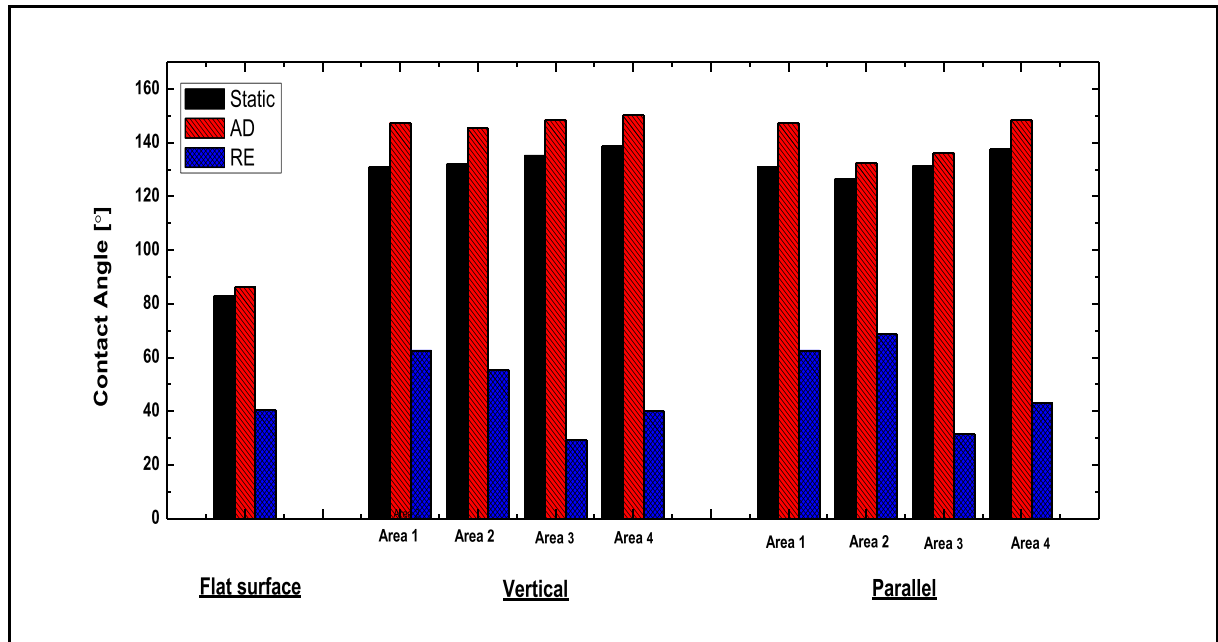


Fig. 5. Contact angle measurements for PVC.

an inclined angle of 53° was used. The size of the structures was controlled by changing the cutting depth. The 53° inclined angle ensured that the width of the gratings was the same as the cutting depth. Mineral spirit mist was used as coolant during the cutting process. To ensure the consistency of the cutting process, all substrates ($75 \text{ mm} \times 25 \text{ mm}$) were mounted circularly around the center of the headstock (Fig. 2(a)). An optical microscope image of the diamond cutting process is shown in Fig. 2(b). On each substrate, gratings in dimensions of $4 \mu\text{m}$, $2 \mu\text{m}$, $1 \mu\text{m}$, and $0.5 \mu\text{m}$ were cut within the ribbon areas 1–4 (Fig. 2(c)). The fabrication results were measured by scanning electron microscopy (SEM; FEI Quanta 3D FEG). To avoid contaminating the surfaces, all samples were uncoated and measured under low vacuum SEM mode (120 Pa).

The wettability of the surfaces was characterized by measuring the contact angles (Krüss Drop Shape Analyzer – DSA30) at different areas

of each sample, along vertical and parallel directions (Fig. 2(c)). To reduce error in measurement, five water droplets ($2 \mu\text{L}$ each) were randomly placed in each area. For each droplet, apparent contact angles including static contact angle, advancing contact angle, and receding contact angle were measured, and the average value was considered the measurement result.

3. Results and discussion

SEM images of the micro and nanostructures from $4 \mu\text{m}$ to 500 nm on different substrates are shown in Fig. 3. Under the same cutting depth, the actual surface topography of the gratings on metal and plastic surfaces slightly differed due to the different elastic recovery rates after material removal.

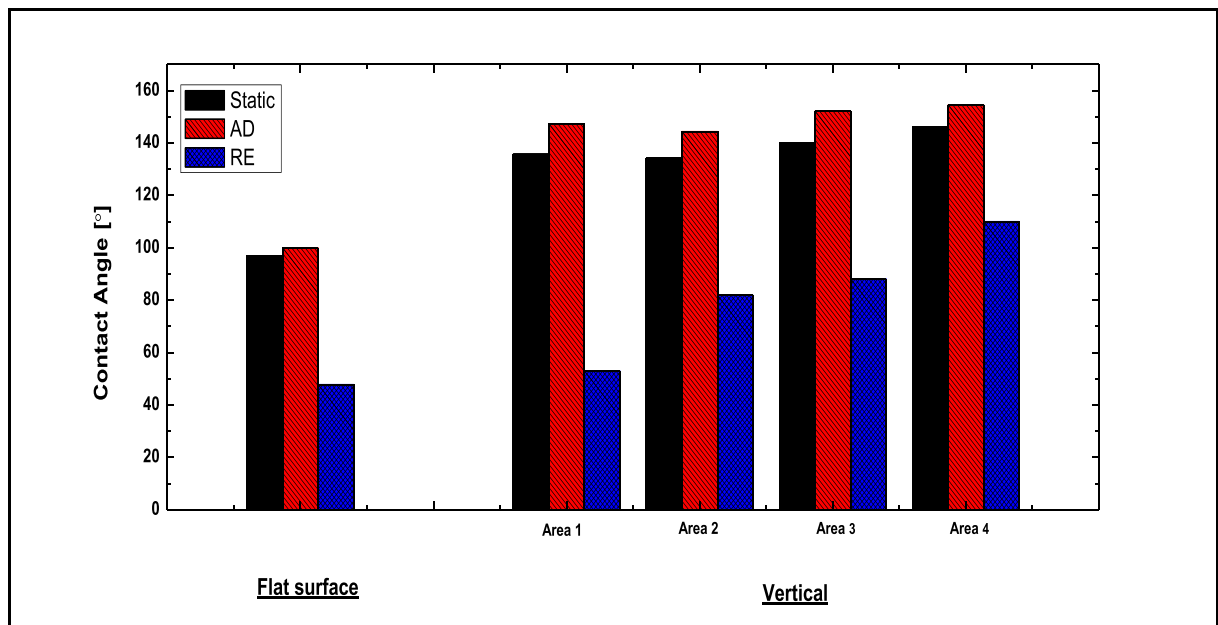


Fig. 6. Contact angle measurements for PE 1000.

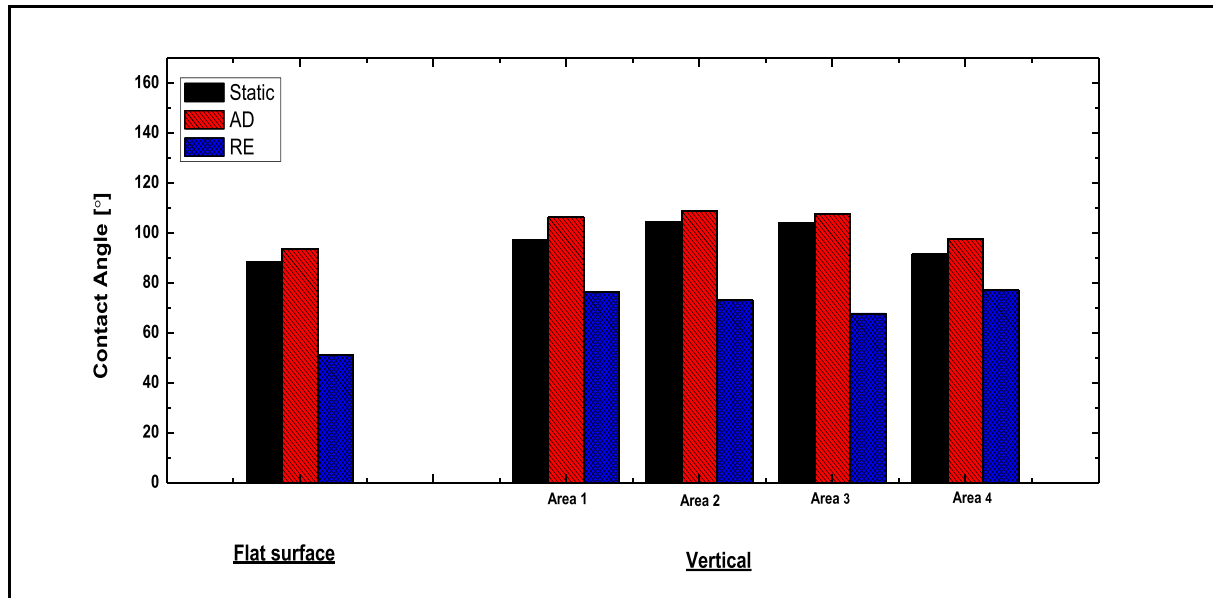


Fig. 7. Contact angle measurements for PE 500.

For each material, contact angles on flat surface and structured surfaces (areas 1–4) were measured. The measurement results for contact angles are shown in Figs. 4–9. For aluminum and PVC, all contact angles were measured along both vertical and parallel directions (Fig. 2(c)). The measurement results for these two materials are illustrated in Figs. 4 and 5.

For each material, the roughness factor (R_f) and packing parameter (p) were calculated. The packing parameter is the fraction of the structured surface area over the total area of the substrate. The roughness factor was estimated theoretically given that the patterns adopt a square shape and considering the height, width, and distance. For the different patterned areas, the distance between patterns was constant, so the pitch distance did not influence the roughness factor. The width of the patterns showed small variations in the different materials due to the different elastic behavior of the materials during the machining process, resulting in minimal changes in the roughness factor.

Therefore, the roughness factor would depend mainly on the height of the patterns. Considering that the height of the pattern ranged from 4 μm to 500 nm, the roughness factor was expected to decrease from Area 1 (pattern height of 4 μm) to Area 4 (pattern height of 500 nm). The roughness factors and packing parameters for different materials are shown in Table 1.

Given the existence of micro and nanostructures, in areas 1 and 3, the wettability of aluminum changed from hydrophilic ($\theta = 69.4^\circ$) to hydrophobic (up to 93.6°). This result contradicts the Wenzel model defined in Eq. (3). The Wenzel model predicts that an increase in the surface roughness for hydrophilic materials can enhance their hydrophobicity behavior and exhibit small apparent contact angles. Thus, air bubbles successfully trapped by these structures possibly affect the wetting behavior of aluminum substrates, and the droplet follows a composite state. If the droplet is in the composite state, the apparent contact angle should be calculated using Cassie and Baxter's model

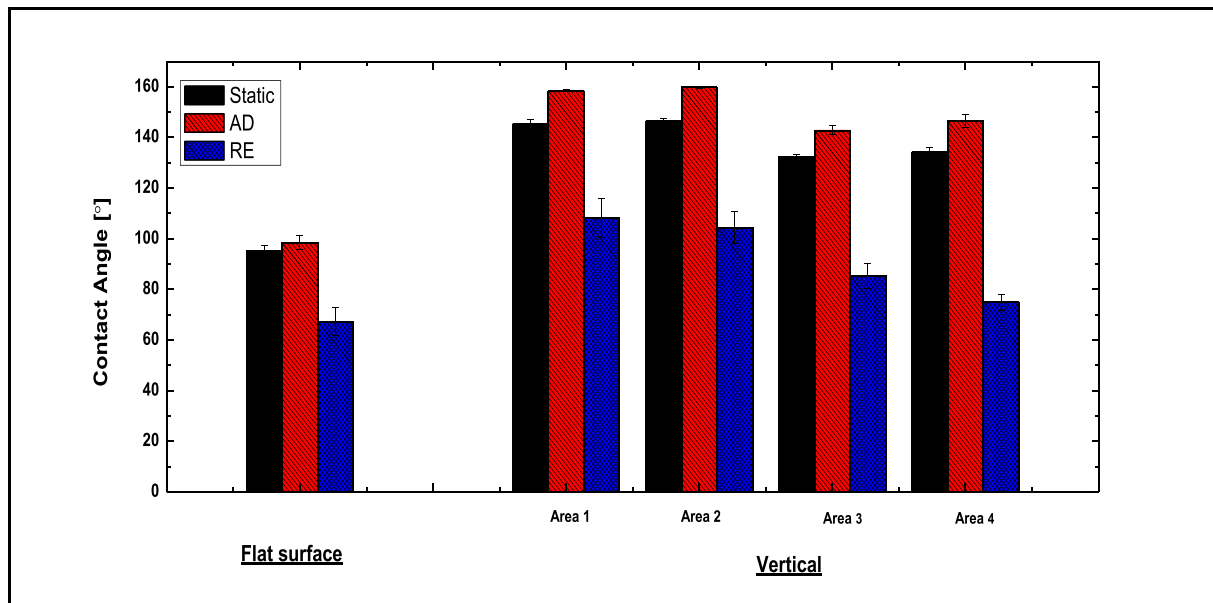


Fig. 8. Contact angle measurements for PP.

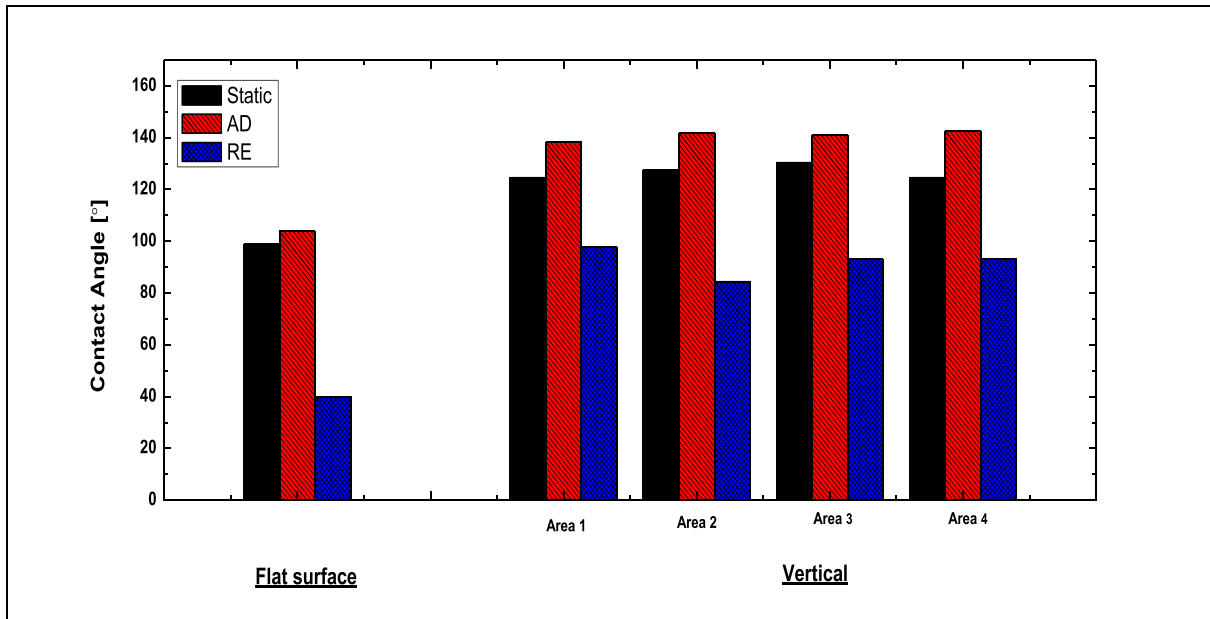


Fig. 9. Contact angle measurements for PTFE.

defined by Eq. (4). Zu et al. performed a theoretical analysis on substrates patterned by square patterns following the Cassie–Baxter model. This model predicts that the area fraction of the solid–liquid interface, f , is only dependent on the pattern width and pitch distance. This model predicts that the apparent contact angle should decrease with the increase in pattern height for flat substrates with $\theta \approx 90^\circ$.²⁴ This model cannot explain the experimental results. These results can be explained by taking into account the phenomenon of passivation where aluminum forms a thin surface layer of aluminum oxide upon contact with oxygen in the atmosphere through oxidation, which is enhanced at high temperatures. This layer creates porosity on the surface of the structures. The formation of this oxidized structure can resemble anodized aluminum. The surface of passivated aluminum transitions from slightly hydrophilic to moderately hydrophobic up to film thicknesses of about 6 μm .²⁵

PVC, PE 1000, PP, and PTFE exhibited a great change in their wettability behavior ($\Delta\theta > 50^\circ$) when micro- and nanostructures were introduced to the surfaces, shifting from non-extraordinary wettability behavior ($\theta \approx 90^\circ$) to superhydrophobic behavior ($\theta \approx 150^\circ$). All four areas with structures ranging from 500 nm to 4 μm showed similar contact angles. The Wenzel model predicts that patterned materials with intrinsic contact angles $\theta \approx 90^\circ$ demonstrate an enhancement in their hydrophobic behavior when the roughness factor is increased. According to Nosonovsky et al., the change in contact angle in the Wenzel model depends on the different geometric parameters of the surface structure such as width and height of the pillars, distance between pillars, patterns shape, and pattern packing.²⁶ This model explains that the aspect ratio and packing parameter of the structures have an outstanding effect on the variation in the contact angle on surfaces with patterned structures. In the different patterned areas, the pattern height decreased from 4 μm to 500 nm, whereas the width of the patterns showed small variations in the different materials due to the different elastic behavior of the materials during the machining process. The aspect ratio was in the range of 1–5 for the different manufactured areas. In the different patterned surfaces, p oscillated between 0.5 and 0.9. According to this theoretical analysis, an increase in the aspect ratio for materials with intrinsic contact angles $\theta \approx 90^\circ$ could extensively enhance the hydrophobicity of the materials.

With the patterned surfaces, the hydrophobicity of PE 500 only slightly increased ($\Delta\theta \approx 10^\circ$ – 15°). According to theoretical analysis, the Cassie–Baxter model indicates that the height of the pillars does

not influence the wettability of the materials.²⁴ This phenomenon is quite unique especially when compared with PE 1000, which has very similar wettability on flat surfaces. This effect can also be explained by their different surface topography. PE 1000 offers higher wear resistance and impact strength than PE 500. Therefore, under the same cutting parameters, PE1000 is more difficult to remove than PE 500. As shown in Fig. 10, the gaps between each patterns (1 μm) on PE 1000 (Fig. 10(a)) were smaller than those on PE 500 (Fig. 10(b)), leading to a void space with high aspect ratio, which facilitated air trapping and resulted in a high contact angle. Thus, for hydrophobic surfaces ($\theta \approx 100^\circ$) of moderate roughness ($R_s \approx 2$), both wettability models can co-exist, and the droplet may stay in a state of metastable equilibrium.²⁴

The contact angle hysteresis of each material is also studied. Theoretical analysis of other researchers demonstrated that contact angle hysteresis depends on the width/pitch ratio of the structures, as well as the density of the pillars.^{27,28} Among the tested materials, aluminum, PE 500, PP, and PTFE did not show a measurable change in contact angle hysteresis with the different patterns, whereas PE 1000 exhibited an enhancement in contact angle hysteresis with an increased the roughness factor. By contrast, PVC showed a reduction in contact angle hysteresis when the roughness factor increased. Our observation revealed a relationship between contact angle hysteresis and the size of the surface structures. Recent research demonstrated that contact angle hysteresis is strongly correlated with the projected area fraction for fully wetting space (f_w).²⁹ For all the polymer materials used in this work, f_w varied from 0 to 1, depending on the structures and surface finish. Although the same size of structures was achieved on different materials, the surface finish differed (Fig. 3). Such a difference caused the unpredictable behavior of contact angle hysteresis on different materials. Other studies indicated that contact angle hysteresis is affected by the height of the patterns, pitch distance,³⁰ and shape of patterns.^{31,32} The main

Table 1
Roughness factor and packing parameter estimation for the different materials.

Material	R_f	p
Aluminum	3.8–4.79	0.84–0.90
PVC	3.9–5.08	0.55–0.96
PE 1000	3.83–4.56	0.76–0.79
PE 500	3.01–4.07	0.54–0.73
PTFE	1.08–2.86	0.76–0.80
PP	2.62–4.12	0.70–0.76

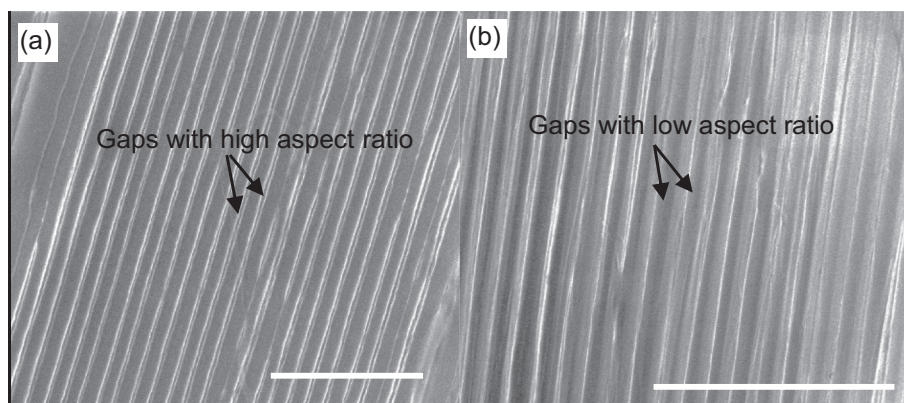


Fig. 10. SEM images of 1 μm gratings on PE 1000 (a) and PE 500 (b) (scale bar is 10 μm).

finding in the literature is that sharp patterns lead to a remarkable enhancement in contact angle hysteresis.³³ Further research should focus on controlling surface finish and the shape of structures for an in-depth study of contact angle hysteresis.

4. Conclusions

By using SPDT, this research demonstrated the changes in surface wettability through micro- and nanostructures on materials that cannot be processed by conventional lithography-based technologies. Results revealed that the wettability of polymers such as PVC, PE 1000, PP, and PTFE can be greatly enhanced ($\Delta\theta \approx 50^\circ$). Meanwhile, aluminum and PE 500 exhibit a moderate change in their wettability properties ($\Delta\theta \approx 10^\circ$) when features are manufactured on their surfaces. From 500 nm to 4 μm , the correlation between the sizes of the structures and surface wettability is not strong. In such a scale, the aspect ratio of void structures plays an important role in surface wettability. For the same material, void space with high aspect ratio can trap air easily, resulting in a high contact angle. In addition, the experimental results can be well explained through the introduction of the roughness factor and the packing parameter, which indicates that surfaces with different wettabilities can be tuned through these parameters and then fabricated by SPDT.

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